Nonhomogeneous Dirichlet Problems for the p-Laplacian

J.-P. Gossez (Bruxelles)

This talk is mainly concerned with the existence, nonexistence and multiplicity of positive solutions for the problem

$$\begin{cases} -\Delta_p \, u = \lambda u^{q-1} \text{ in } \Omega, \\ u = \varphi \text{ on } \partial \Omega. \end{cases}$$
(1)

For $p = 2, q = p^*$ and $\varphi = 0$, this is the well-known Pohozaev equation, which has lead to a very large number of works dealing with criticality. Our purpose here is to study problem (1) in the case of the *p*-Laplacian with a nonzero boundary data φ .

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